

THOMSON SCATTERING

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- ❑ Introducing me
- ❑ Thomson scattering – Principles
- ❑ Thomson scattering – Experimental setup
- ❑ Main instrumental strategies how to measure profiles of T_e and n_e
- ❑ Examples of TS diagnostics at fusion devices
- ❑ Good to think of
- ❑ Challenges
- ❑ New trends

- Mathematic – Physics Faculty, Charles University, Prague. PhD in Experimental physics – Low temperature plasma, thin layers
- NATO grant – magnetron sputtering, producing ZnO and BN layers and its characterization
- Institute of Physics – Liquid crystals
- Institute of Plasma Physics – High temperature plasma physics and fusion. Task: build Thomson scattering
- First trip was to TEXTOR tokamak – supervision of Mikhail Kantor and Roger Jaspers
- Second trip was to MAST – supervised by Mike Walsh and Rory Scannell
- I met many great Thomson scattering people through the years – conferences, experiments
- I came to the IPP to do a research but I was asked to build the diagnostics system first
- Instrumentation is an important art. There is no perfect fusion research without good diagnostics.
- Thomson scattering can be simple but it is not easy (no big mistakes allowed on the road ...)
- Therefore, life of “Thomsonists” is never boring

Acknowledgement:

M.Leyland (University of YORK & CCFE, Culham Science Centre – MAST and JET)

M.J.Walsh (ITER, Head of Diagnostics)

R.Scannell (CCFE, Culham Science Centre, MAST, Thomson scattering)

Gas in thermal equilibrium (f.e. in a room) – most probable **velocity distribution** of the particles is Maxwellian

1D **Maxwellian** velocity distribution:

$$f(v_x) = A \cdot e^{-((1/2)mv_x^2)/k_B T}$$

Normalisation: density $n = \int_{-\infty}^{\infty} f(v) dv$

$$A = n(m/(2\pi k_B T))^{1/2}$$

Typical velocity of N₂ at 300K:

$$1/2m\mathbf{v}^2 = 1/2k_B\mathbf{T}$$

at 300 K : $v = 0.30 \text{ kms}^{-1}$

Different temperature would change the velocity.

Maxwellian can be generically expressed as a Gaussian:

$$f(x) = 1/(\sigma(2\pi)^{1/2}) \cdot e^{-(1/2)(x-x_0)^2/\sigma^2}$$

x_0 mean

σ standard deviation

related to width of Gaussian

1D: $\sigma = (k_B T/m)^{1/2}$, $x_0 = 0$

$1/2 m v^2 = 1/2 k_B T \Rightarrow v = \sigma$

Can determine σ from Gaussian and relate the width to temperature, i.e.

width of the Maxwellian is determined by the constant T called temperature.

Temperature quoted in energy units:

$$T_e = 1\text{keV} \approx 10\,000\,000\text{ K}$$

Plasma – quasi neutral gas of ions, electrons, neutrals

We assume a **Maxwellian distribution of electron velocities**

(Just remind):

Wave: $A(\theta) = B \cdot \cos(\theta)$

θ phase, A amplitude, B constant

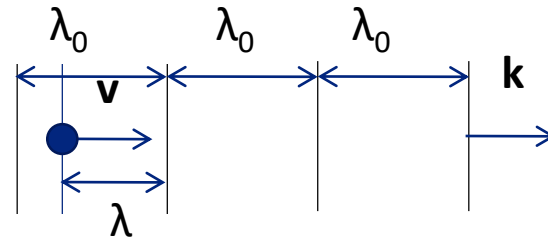
k vector: $k = d\theta/dx$

$A(x) = B \cdot \cos(kx + \varphi)$

1 cycle $\Delta \theta = 2\pi$, $x = \lambda$ $k = 2\pi / \lambda$

$\omega = 2\pi/T = 2\pi f$

Doppler shift:



$$\lambda = \lambda_0 - v \cdot T$$

Source emitting wave (λ_0) is moving at a velocity v
 λ is compressed by the distance the source travels
 in 1 period

shortening λ – blue shift
 extending λ – red shift

Doppler shift:

$$\lambda = \lambda_0 - v \cdot T = \lambda_0 - v \cdot \lambda_0 / c = \lambda_0 (1 - v/c), \quad T = 1/f = \lambda_0 / c$$

$$\Delta \lambda = \lambda - \lambda_0 = \lambda_0 (1 - v/c) - \lambda_0$$

$$\Delta \lambda / \lambda_0 = -v/c$$

$$\Delta \omega / \omega_0 = v/c$$

Positive shift in λ results in negative shift in ω .

$$\Delta \omega = \omega_0 \cdot v/c = (2\pi / \lambda) \cdot v = \mathbf{k} \cdot \mathbf{v}$$

More generically $\Delta \omega = \mathbf{k} \cdot \mathbf{v}$

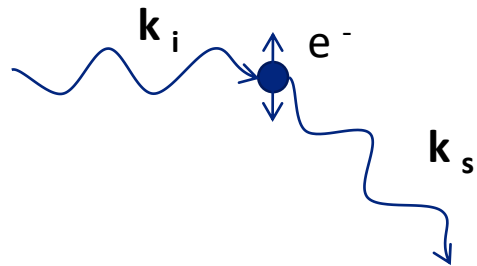
The frequency change due to Doppler shift is equal to the dot product of the \mathbf{k} vector and the velocity of the source.

Scattering:

Classical – absorption & re-emission

$$\hbar \omega \ll mc^2$$

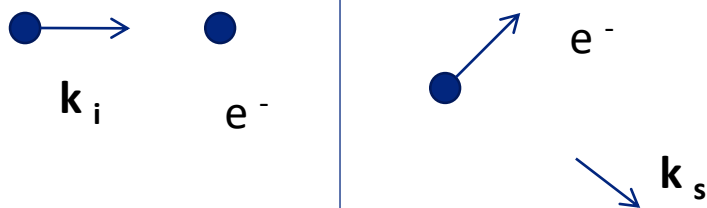
THOMSON SCATTERING



Quantum – collision of particles

$$\hbar \omega \gg mc^2$$

COMPTON SCATTERING



Scattering regimes on free electrons:

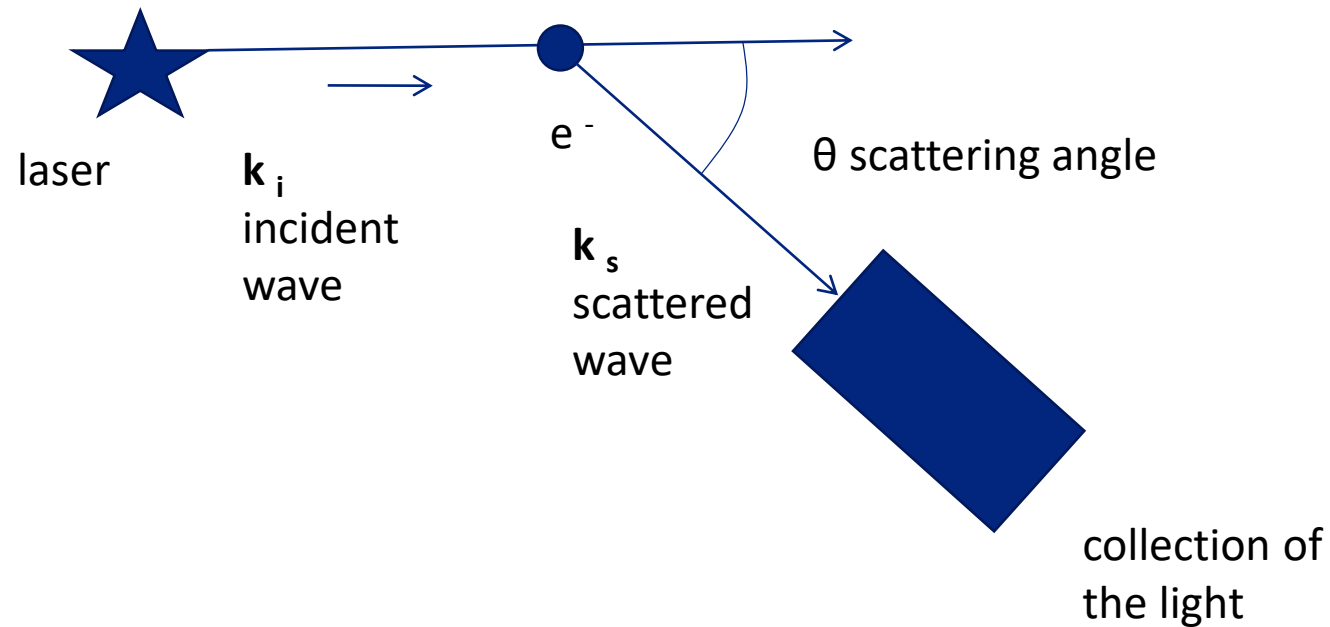
$$e^- : mc^2 = 0.51 \text{ MeV}$$

$$\text{Nd:YAG lasers } (\lambda = 1064 \text{ nm}) : \hbar \omega = 1.17 \text{ eV}$$

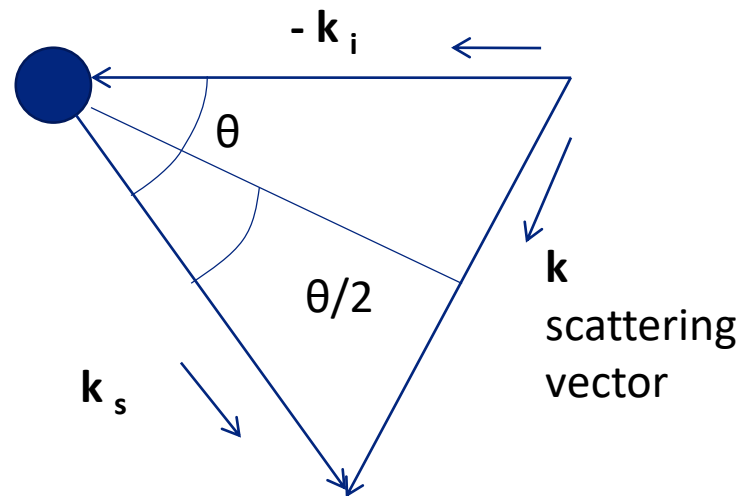
$$\text{Ruby lasers } (\lambda = 694.3 \text{ nm}) : \hbar \omega = 1.79 \text{ eV}$$

Both Thomson scattering regimes.

Typical experimental setup for Thomson scattering



Geometry:



$$\mathbf{k} = \mathbf{k}_s - \mathbf{k}_i$$

$$k_s = k_i = 2\pi/\lambda_0$$

$$\sin \theta/2 = (k/2)/k_s$$

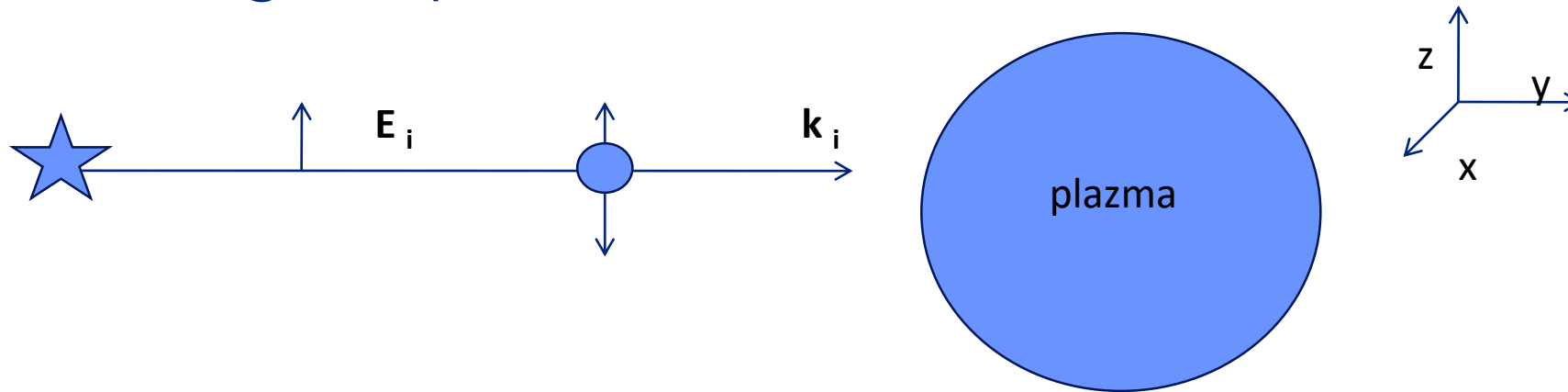
$$k = 2.k_s.\sin \theta/2$$

remind:

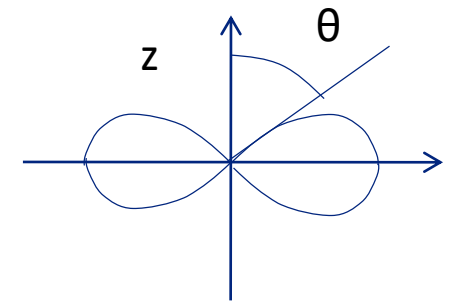
$$\Delta\omega = \mathbf{k} \cdot \mathbf{v}$$

$$\Delta\omega \approx \sin \theta/2$$

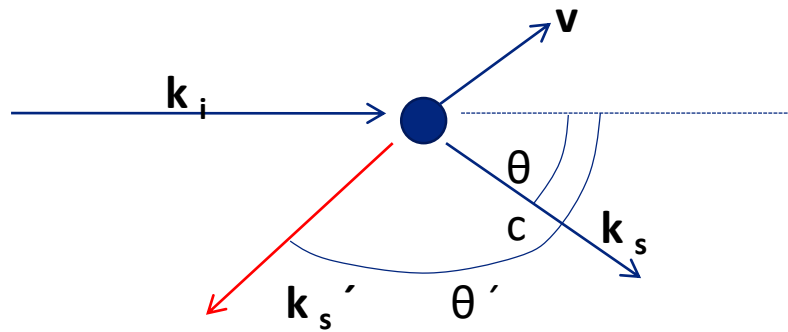
Laser light is polarized:



E_i oscillates in a z direction
 electron oscillation also in a z direction
 re-emitted wave not in direction of oscillation,
 defined by **differential scattering cross-section**
 $d\sigma/d\Omega = r_e^2 \sin^2 \theta$

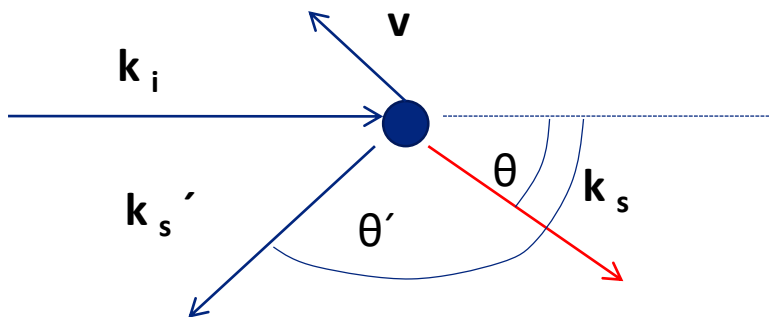


$$\mathbf{v} \cdot \mathbf{k}_i > 0$$



incident wave **red shift** on absorption
 scattered wave **blue** or **red shift** on re – emission
 dep. on θ
 remind: $\Delta \lambda \sim \sin \theta/2$
 $\theta = 0^\circ$ no shift, $\theta = 180^\circ$ double red shift

$$\mathbf{v} \cdot \mathbf{k}_i < 0$$



incident wave **blue shift** on absorption
 scattered wave **blue** or **red shift** on re-emission
 dep. on θ
 $\theta = 0^\circ$ no shift, $\theta = 180^\circ$ double blue shift

remind $\Delta\omega = \mathbf{k} \cdot \mathbf{v} = k \cdot v_k$
 $-\Delta\lambda/\lambda_0 = \Delta\omega/\omega_0$
 $-\Delta\lambda/\lambda = 2 \cdot (v_k/c) \cdot \sin(\theta/2)$

Maxwellian in k vector:

$$f(v_k) = (m/(2\pi k_B T))^{1/2} e^{(-1/2 m v_k^2)/k_B T}$$

$$v_k = -c(\lambda - \lambda_0)/(2 \lambda_0 \sin(\theta/2))$$

Experiment to measure scattered signal as a function of λ . Map velocity space to wavelength space.

Looking for distribution function in terms of λ

$$f(\lambda) = A.e((-1/2(\lambda - \lambda_0)^2/\sigma^2))$$

Standard deviation :

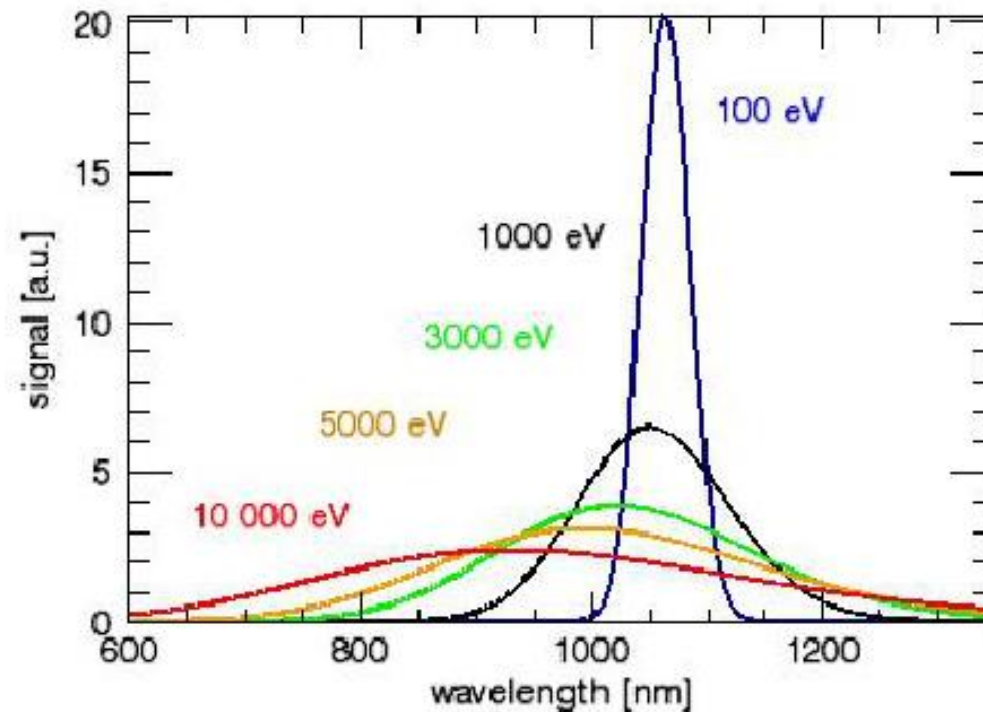
$$\sigma = 2\lambda_0/c(k_B T/m)^{1/2}.\sin(\theta/2)$$

width of scattered peak – temperature T

f.e. 90° , $T_e = 100\text{eV}$, $\lambda = 1064\text{ nm}$ $\sigma = 36\text{ nm}$

High temperatures – high velocities – relativistic effects

Propper code has to be used – Selden Matoba



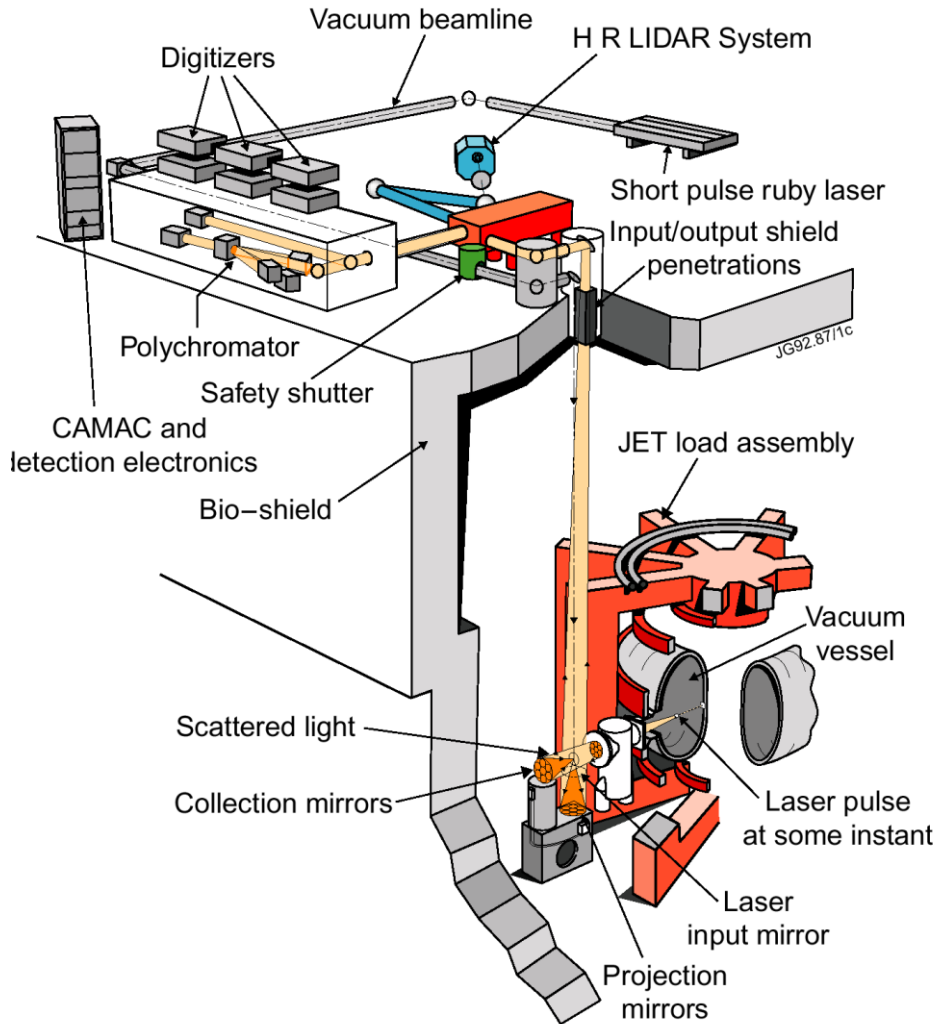
SeldenMatoba code, MAST, UK

Thomson scattering diagnostics is widely used in the fusion community to measure profiles of electron temperature and electron density simultaneously.

The temperature (of electrons) can be calculated from the width of a scattered signal.

The density can be evaluated after comparing scattered signal on free electrons in plasma with scattered signal of radiation by gas molecules

- **Conventional diagnostics**
 - Signal from a laser scattered in a plasma passing a series of spectral filters, Avalanche photodiodes and fast digitizers (GS/s as a laser pulse is only 7 ns long)
 - Signal from a laser scattered in a plasma is lead to a large spectrometer and CCD camera
- **LIDAR diagnostic**



JET's LIDAR – TS Diagnostics on the roof of the Torus HALL

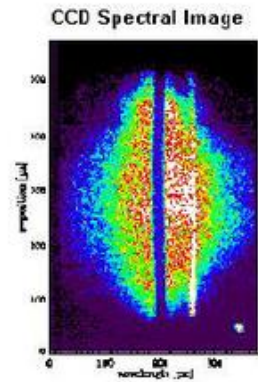
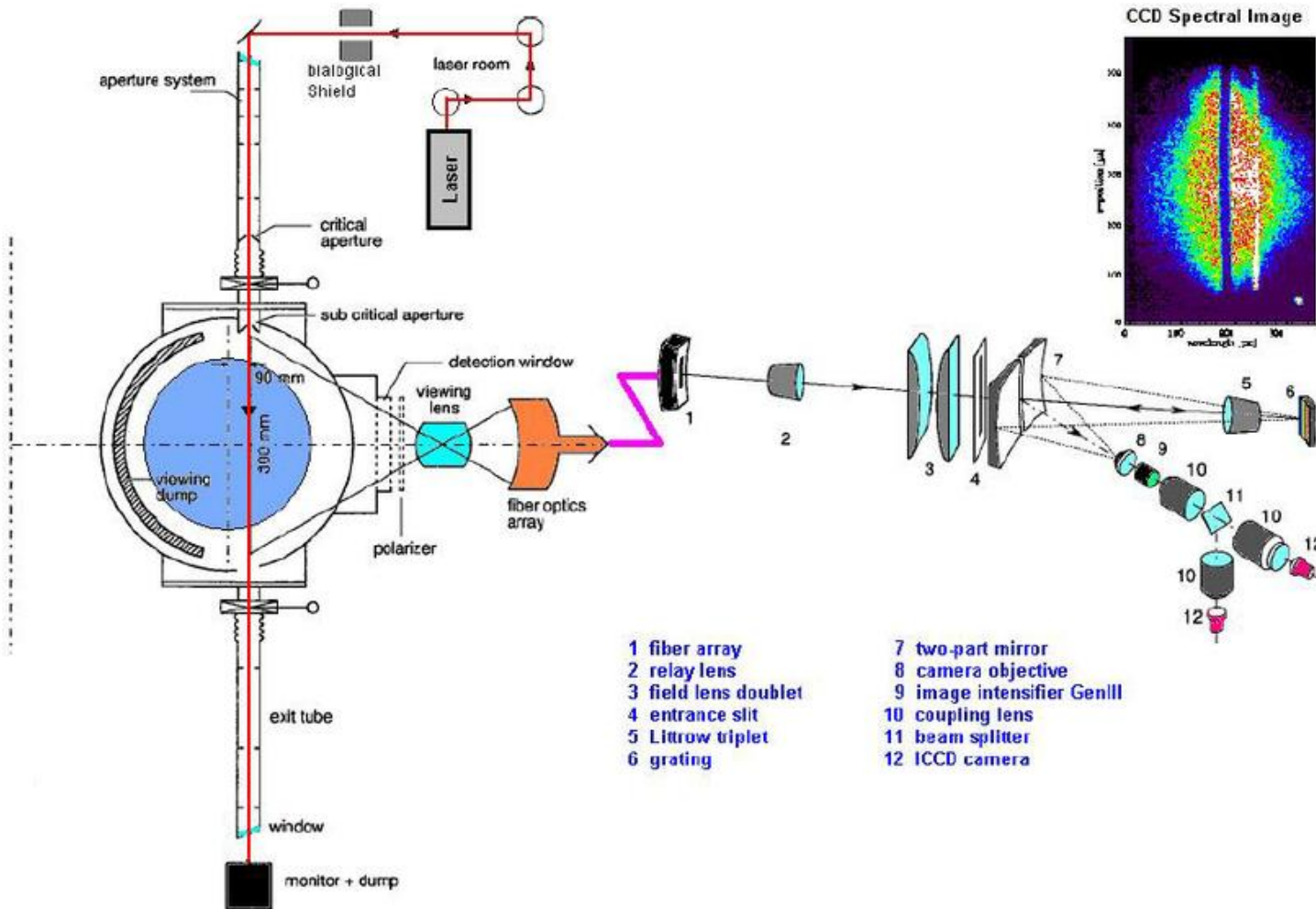
„Light Detection And Ranging“

180° scattering

Short pulses (300 ps \propto 9 cm)

Time-of-flight

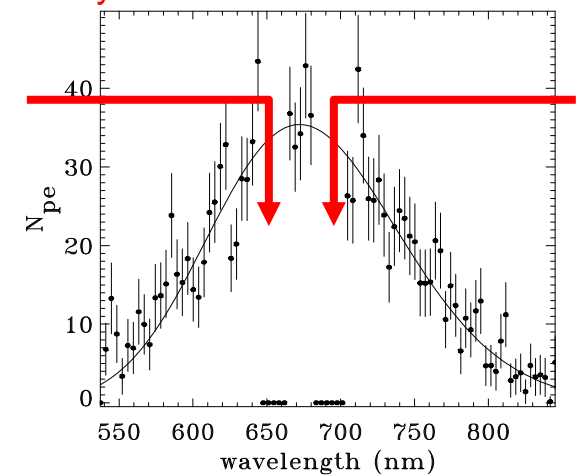
→ position information



Schematic layout of the double-pulse Thomson scattering at the TEXTOR tokamak

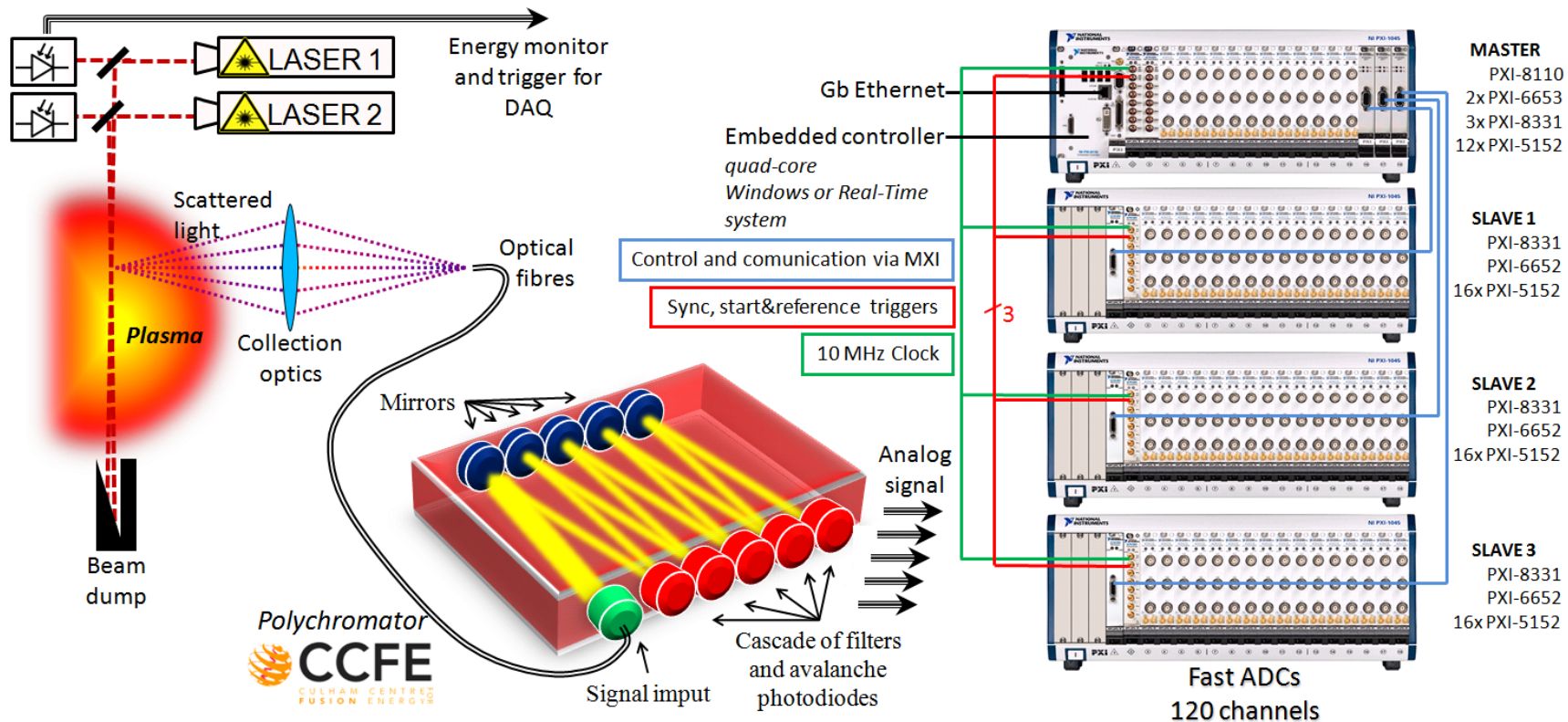
H_{α} -emission is cut away

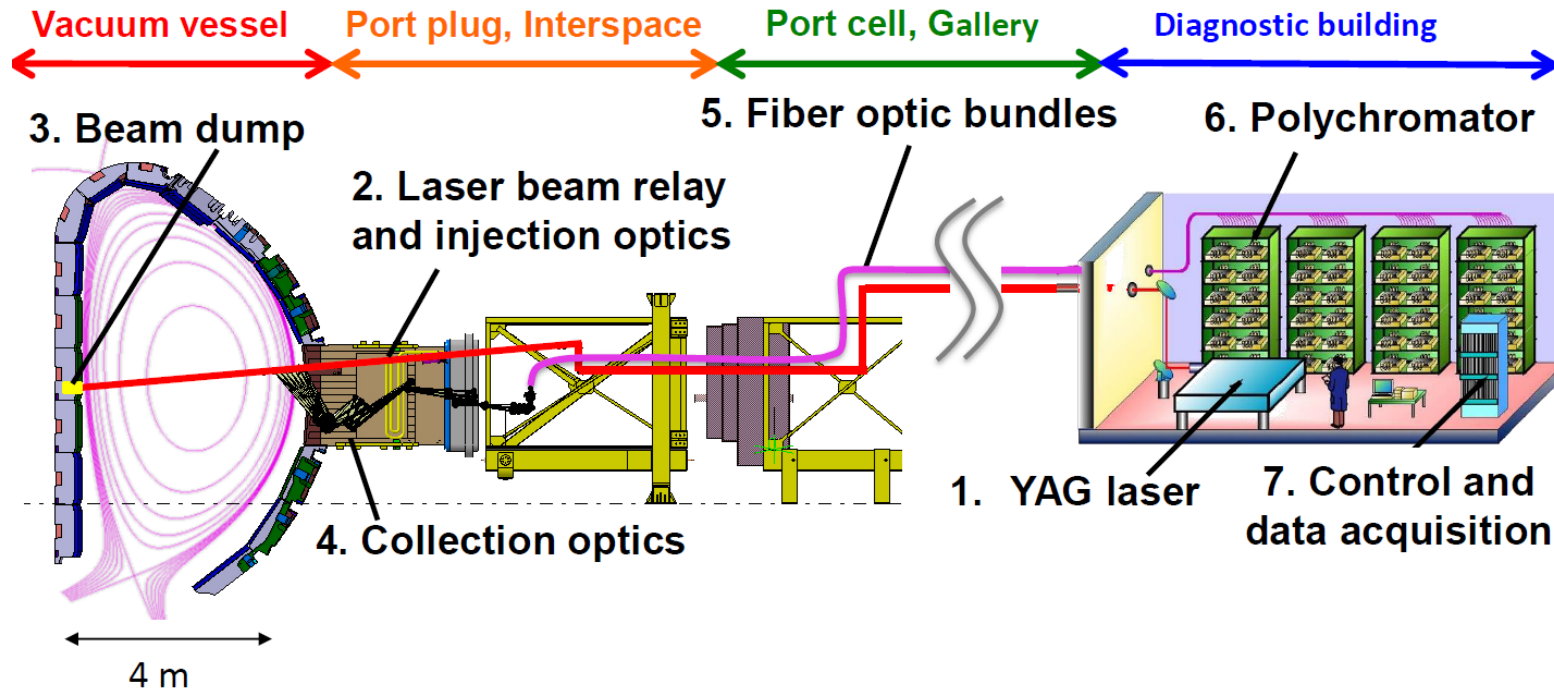
Laser wavelength is cut out



[R. Jaspers, M. Kantor, TEXTOR]

Filters and APDs solution, laser 1064 nm @ 1.5 J
 This system is used at tokamaks COMPASS, MAST, JET





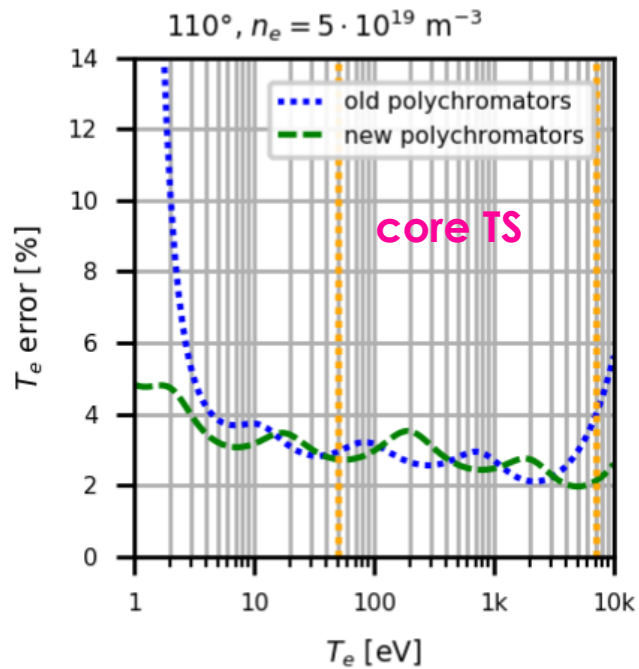
- Nd:YAG laser, fiber optical bundles, polychromators
- Final design review of the laser beam dump 2022
- Next FDR about components in tokamak building planned for June 2025
- Beam dump – extreme heat load 2,4 kW – plasma spray coating of ceramic applied on stainless steel (20 micrometer $\text{Al}_2\text{O}_3\text{-TiO}_2$ coating samples tested)

[Courtesy: Eichii Yatsuka, ITER Japan Domestic Agency]

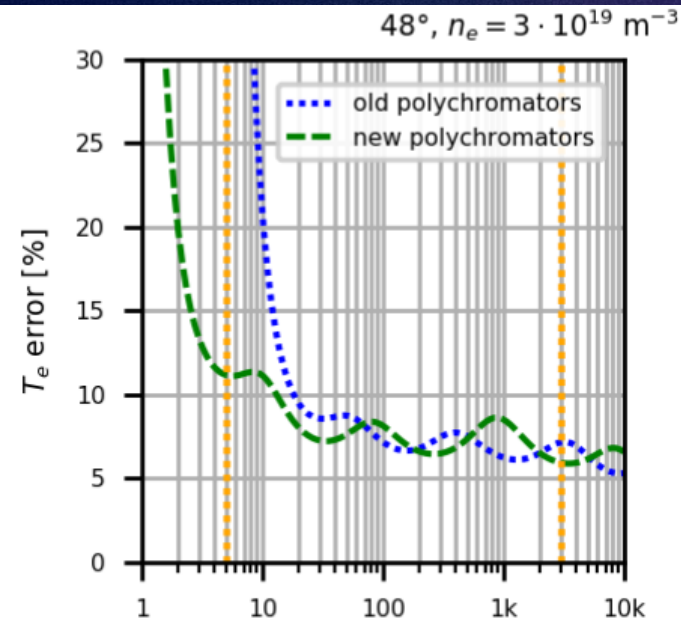
- **Choice between conventional TS and LIDAR**
 - LIDAR – simpler optics and more robust but requires more advanced detectors
 - Conventional TS based on Avalanche photodiodes detection more common
- **Fiber bundle cross-section** dimensions at the tokamak side
 - Dimension alongside the laser line – smaller one gives better spatial resolution but lower signal (critical for TS)
 - Dimension across the laser line – bigger one provides a better clearance in case of laser misalignment but collects more background light (worse signal/noise ratio)
- **Choice of spectral filters**
 - To cover the requested spectral range
 - To optimize error curve versus range of measured T_e , n_e
 - More filters – smoother curve but higher losses through the system. Usually not more than 6 filters are used for that reason.

Example – Optimization of spectral filters choice for COMPASS Upgrade

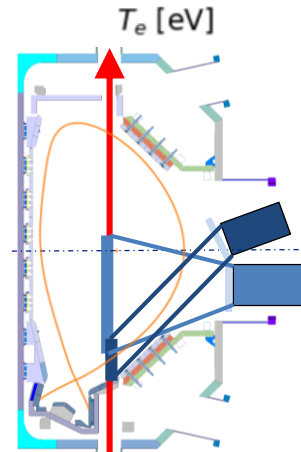
- optimization of filters for both
 - edge TS
 - low T_e
 - orientation of optics
-> variable scattering angle
 - core TS – high T_e



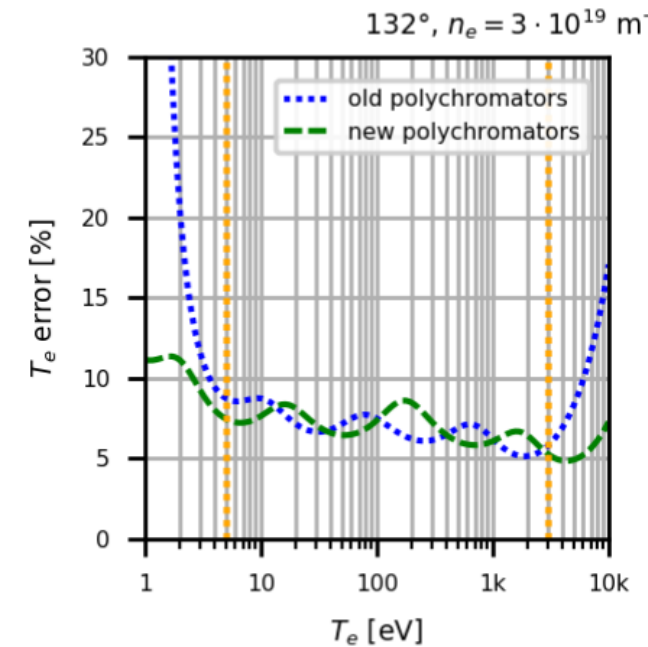
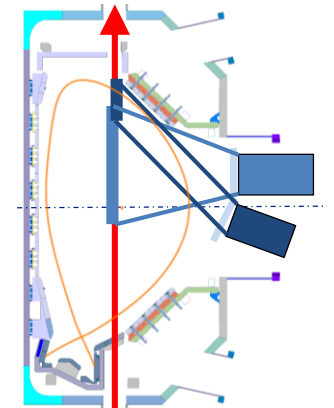
[P. Böhm, IPP.CR]



edge TS - bottom

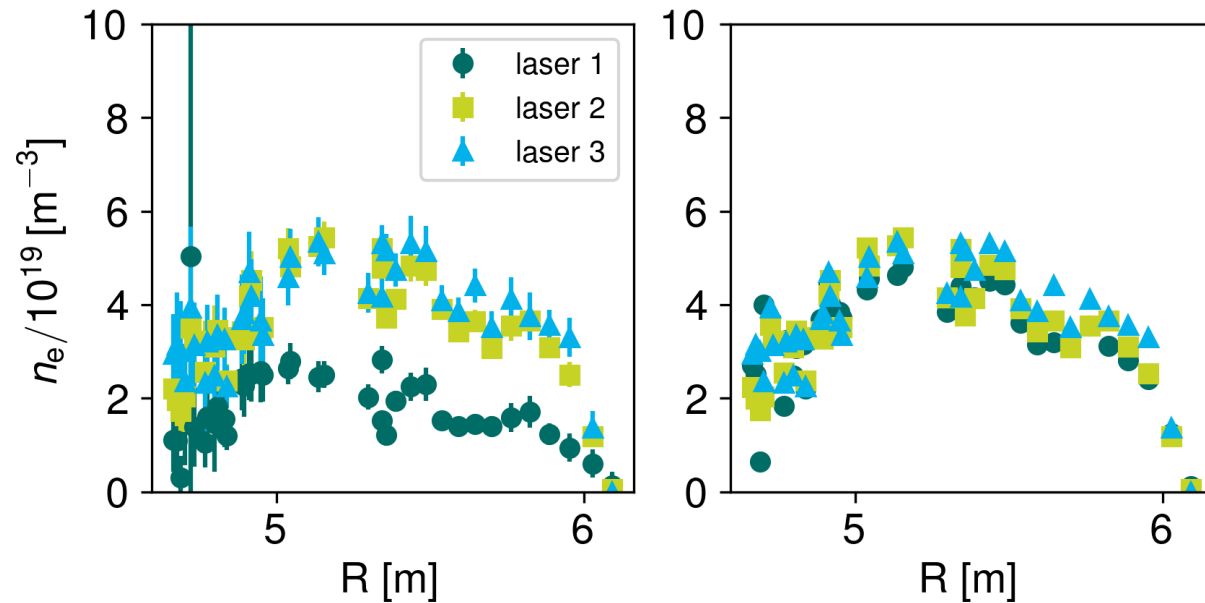


edge TS - top



- Laser line stability, laser position monitoring
- Alignment – misalignment leads to an incorrect n_e calculation
- Calibrations – absolute, spectral
- Strategy how to maintain a good quality of measured data when access to the experimental device during experimental campaign is limited:
 - Remote alignment
 - Calibration during experimental campaign
 - Using neural network
- Real time

- Absolute Raman calibration depends on laser position.
- Varying the laser position during the calibration → ideal calibration for every position.
- Position monitoring during TS operation allows choice of correct calibration factor.
- Effect can also be learned from the profile data using machine learning.



[Fuchert et al., JINST **17** (2022)]



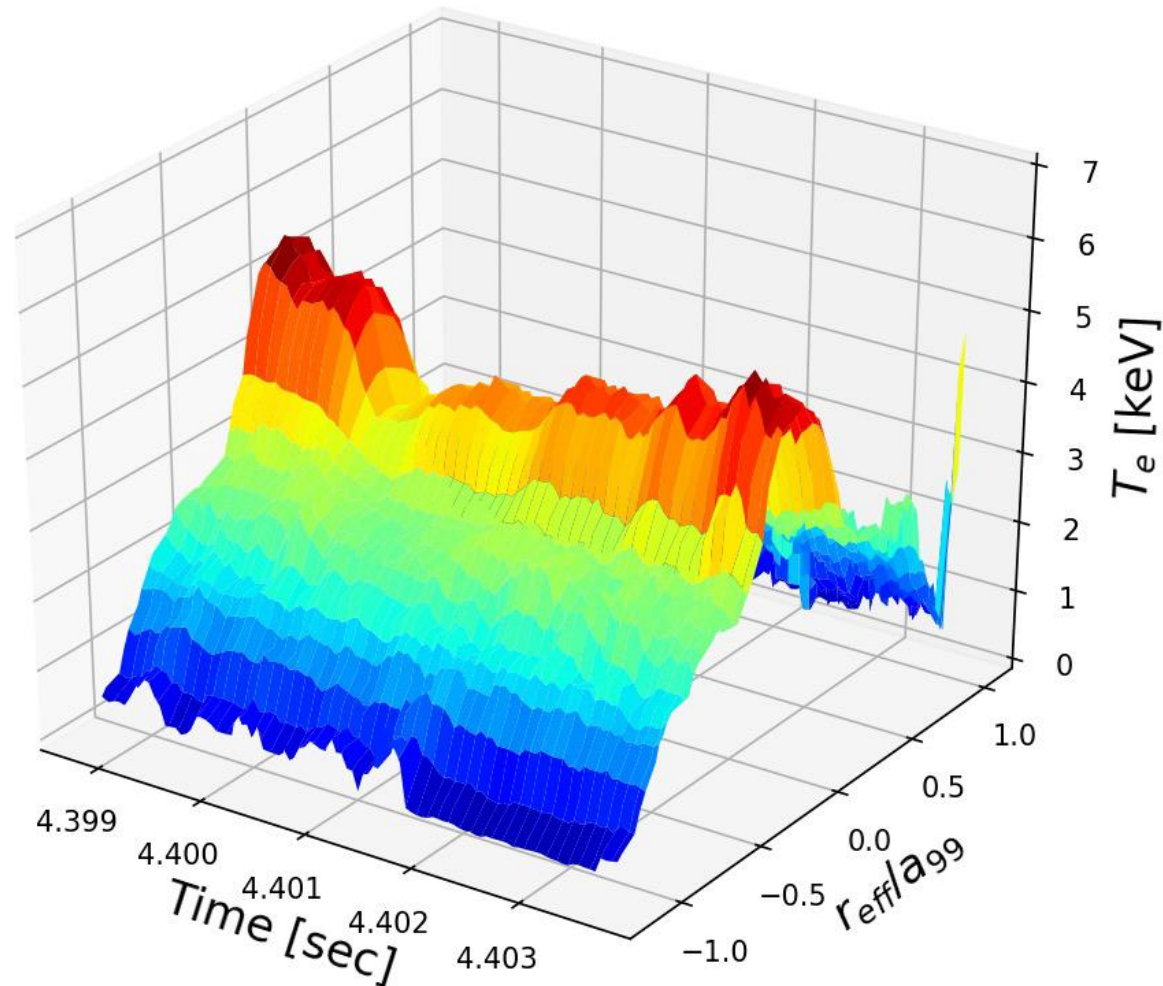
○ Temporal resolution of the TS diagnostics

- Laser has to have a high power output – conventional lasers off the shelf offer only tens of Hz repetition rate which is not sufficient to capture fast events in the plasma
- What to do?
- **Sequence of lasers** firing with a very short time delay (MAST-U, COMPASS, ...) – microsecond delay
- Development of a special **High repetition TS system** allowing burst mode (University of Wisconsin @ Daniel Hartog) – up to 100 kHz

High repetition laser system has been built for LHD by Daniel Hartog & team

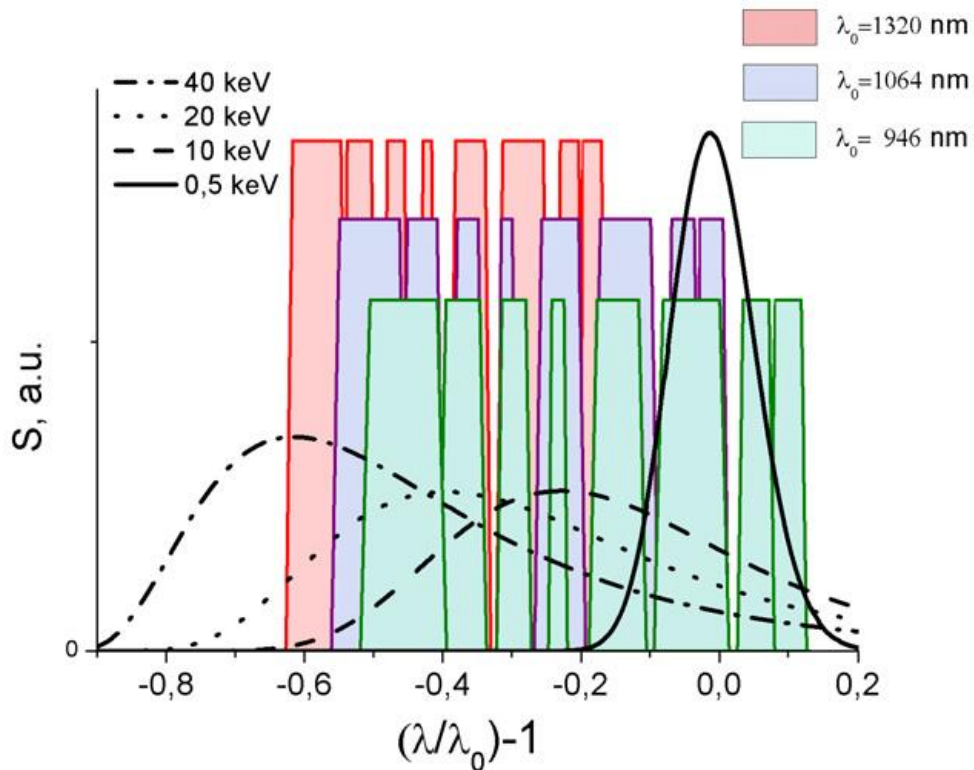
Heat-capacity laser operation – burst of pulses is of limited duration • burst length ≤ 100 ms • pulse rep rate ≥ 1 kHz

High-rep-rate lasers enable detailed measurements of plasma dynamics Example 20 kHz Thomson scattering electron temperature measurement in LHD stellarator (Japan) – captured T_e evolution during minor collapse of e-ITB N. Kenmochi



[N. Kenmochi *et al.*, *Sci. Rep.* **12**, 6979 (2022)]

○ **Too wide a range of measured T_e**



See [G.S. Kurskiev et al 2015 Nucl. Fusion 55 053024]

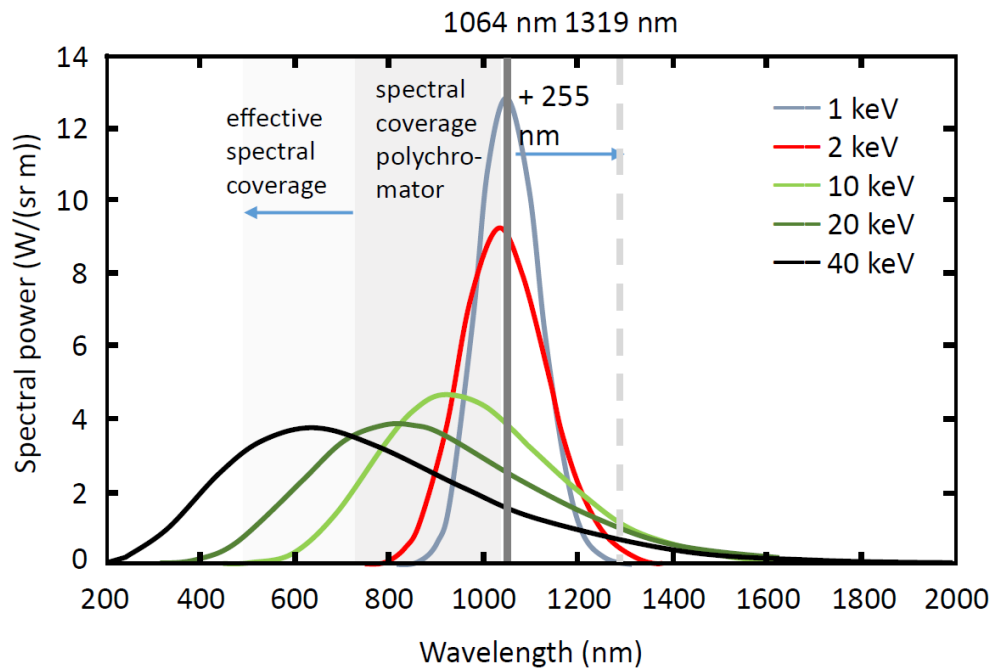
At **high temperatures** ($T_e > 10$ keV, expected to be regularly achieved in **ITER**), the TS **spectrum spans a wide region of wavelengths**.

Spectra widening will be particularly **problematic** in the **core** region, where the **highest temperatures** are expected.

Depolarization effect plays the non-negligible role

What to do?

1) High T_e measurements using dual-wavelength TS

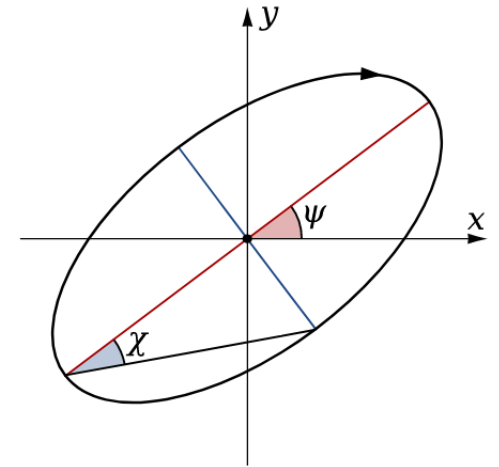


[E. Pasch et al, *Rev. Sci. Instrum.* 89, 10C115 (2018)] and [E. Pasch et al, Recent progress of dual-laser wavelength Thomson scattering, poster contribution at HTPD24]

- This technique allows to **expand** the **detectable spectrum** by using **two lasers** at **different wavelength**.
- **1064 nm** and **1319 nm** lasers (5 J and 2 J, respectively)
- Allows for **in-situ calibrations** by **measuring** the **relative sensitivities** of **spectral channels** with two-lasers
- **Higher temperature** can be measured
- This system is **currently** being **tested** in **W7-X** (see, for instance, [F.A. D'Isa et al 2023 JINST 18 C11025])

2) Polarimetric TS

- Measures depolarization of the scattered light
- Degree of depolarization as a function of T_e
- When a completely polarised source (such as the TS input laser) is injected into a high temperature plasma, the scattered radiation collected by TS systems will be partially depolarised.
- This is a relativistic effect (see [V. V. Mirnov, D. J. Den Hartog, and E. Parke, Phys. Plasmas 23, 052108 (2016)]), i.e. it is non-negligible only at high temperatures (see also [R. Scannell et al, Rev. Sci. Instrum. 94, 013506 (2023)], where recent measurements of depolarisation in JET are reported).
- Using Mueller matrices formalism, the degree of depolarisation can be written as a function of multiple factors (scattering angle, orientation and ellipticity of the polarisation ellipse, electron temperature)
- The choice of θ_{scat} , χ , ψ , T_e strongly affects the system feasibility

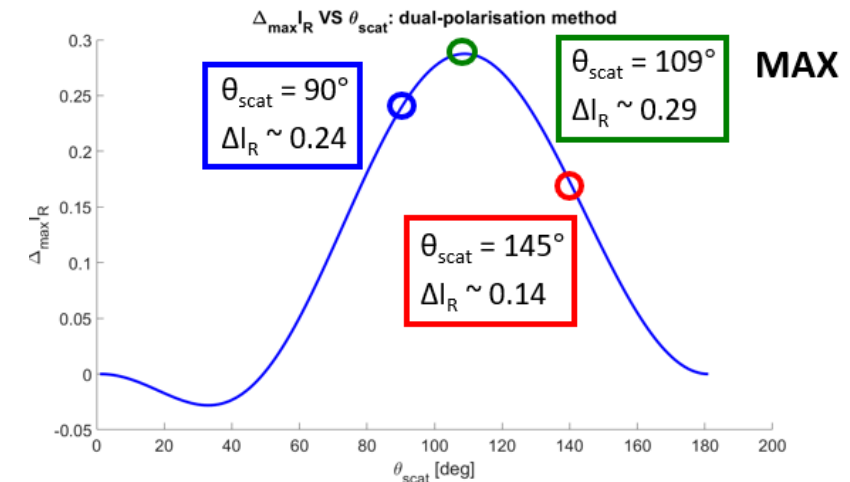


$$D = D(\theta_{scat}, \chi, \psi, T_e)$$

[courtesy: Filippo Bagnato, ITPA TG, ITER Organization],
[F. Bagnato et al., Rev. Sci. Instrum. 95, 083506 (2024)]

3) Dual polarization technique

- Technique first proposed by L. Giudicotti and then reported in [H. Tojo Fusion Engineering and Design 191 (2023) 113511]
- injecting a sequence of two laser pulses, one with linear horizontal polarisation (s-laser, linear horizontal polarization), the other vertical (p-laser, linear vertical polarization).
- As the two lasers share the same optics, the optical transmission cancels out in the ratio.
- The ratio between the p and s-laser intensities is measured in output: $I_R = S_{out}^{(ver)}/S_{out}^{(hor)}$
- The s-laser produces a large amount of scattered light. On the other hand, the p-laser produces a significant amount of scattered light only at high temperature.
- Using Stokes vectors formalism and the Mueller matrix derived in [V. V. Mirnov, D. J. Den Hartog, and E. Parke, *Phys. Plasmas* 23, 052108 (2016)], the output ratio I_R is obtained in the form from which T_e and scattering angle can be obtained



Variation of I_R (ΔI_R) between 0 and 50 keV **as a function of θ_{scat}**

[courtesy: Filippo Bagnato, ITPA TG, ITER Organization],
[F. Bagnato et al., *Rev. Sci. Instrum.* 95, 083506 (2024)]

- Using **forward and backward models** to help both diagnostics design process and an efficient data processing (checking for errors, speed – real time)
- Fully **data driven models** can be alternative to avoid uncertainties of physics-based models
- Synthetic diagnostics
- Combining TS and other diagnostics for **synthetic “super resolution” diagnostics**
 - Correlations among diagnostics can be learned using historical data
 - find hidden physics with AI-based multi-modal super resolution
 - ***TS measurements can be created at points where it was not done!***
 - example: evidence of RMP induced island mechanism on the plasma boundary in DIII-D [Jalalvand, arXiv:2405.05908v3 [physics.plasm-ph] 27 Jun 2024]

Thank you for your attention.